# RATIONAL EXPECTATIONS ECONOMIETRICS

Lars Peter Hansen & Thomas J. Sargent



UNDERGROUND CLASSICS IN ECONOMICS

## Rational Expectations Econometrics

Lars Peter Hansen and Thomas J. Sargent

WITH CONTRIBUTIONS BY
John Heaton, Albert Marcet
and William Roberds

#### Underground Classics in Economics

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